

A variational principle for multiply-connected domains in Domino world.

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Aztec diamond of order N , $AD_N := \{(x, y) \in \mathbb{Z}^2 \mid |x| + |y| \leq N\}$

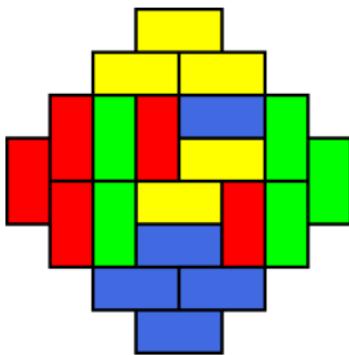


Рис. 1: Aztec diamond AD_4 .

Typical domino tiling

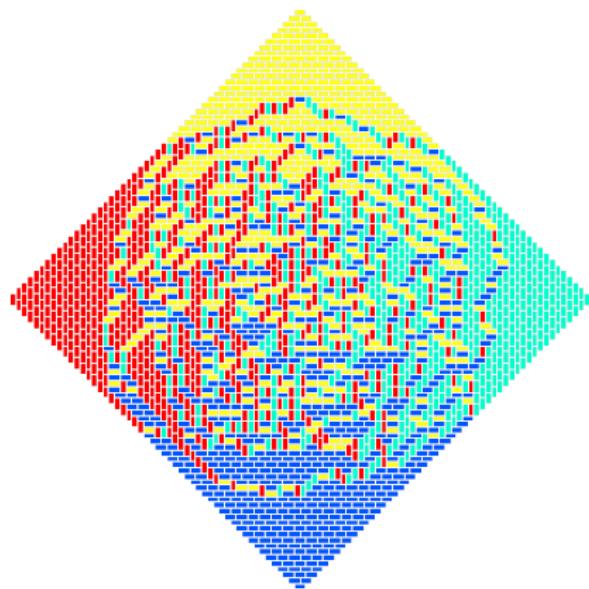


Рис. 2: Typical domino tiling of large Aztec diamond.

Height function. Intuition.

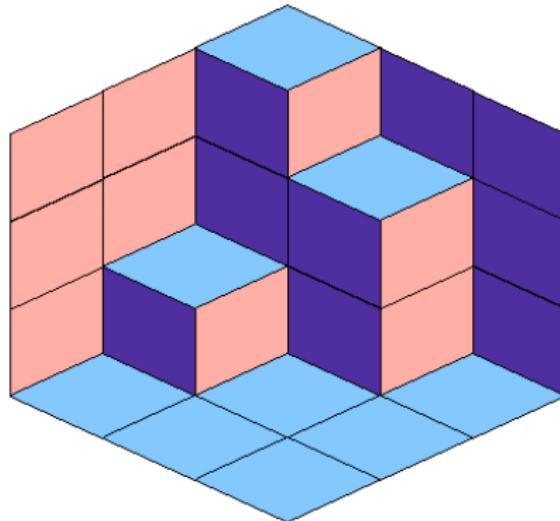


Рис. 3: A lozenge tiling

Height function

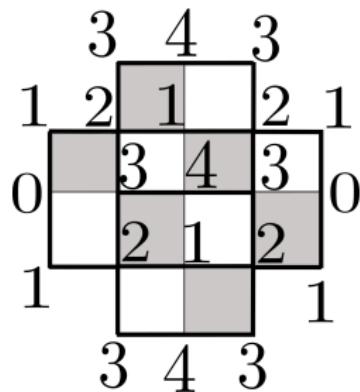


Рис. 4: Height function of Aztec diamond AD_4 .

Limit shape for Aztec diamond

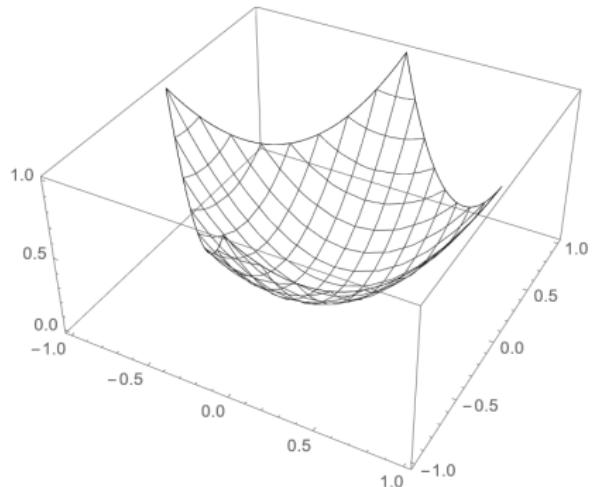


Рис. 5: Plot of h^* for the Aztec diamond

"Riemannian Surface"

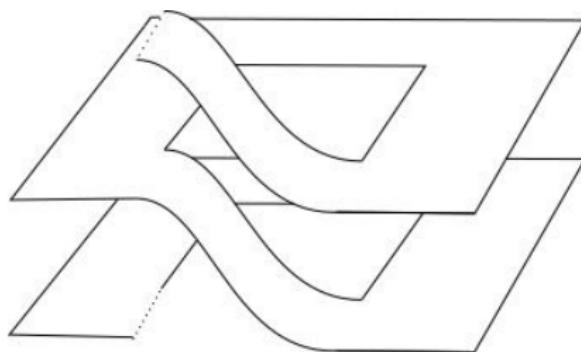
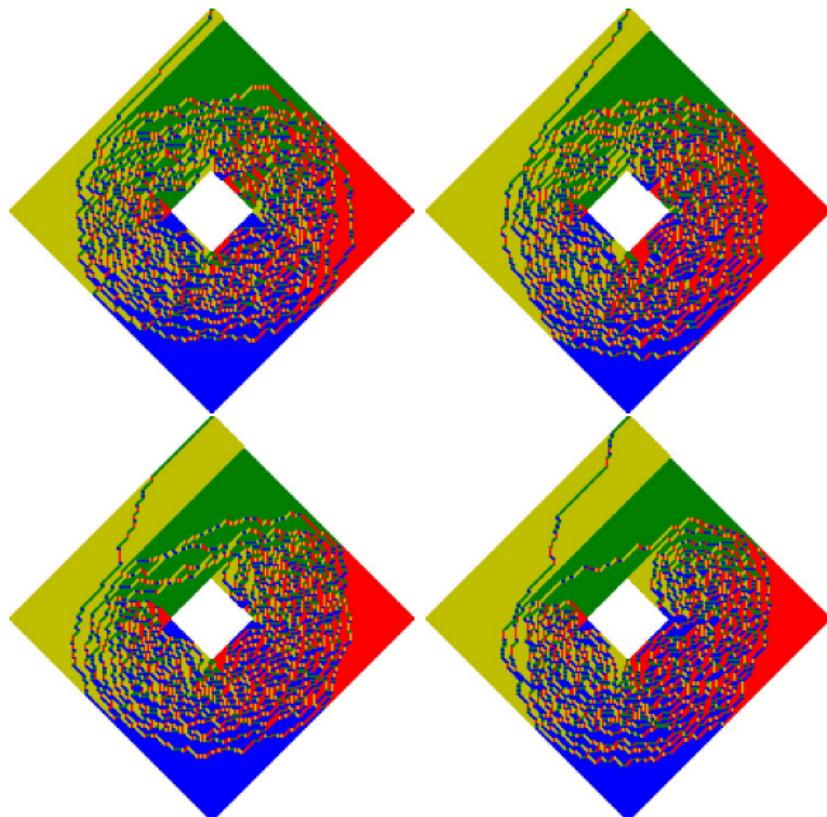


Рис. 6: Two sheets of the surface

Simulations



Modified Aztec diamond I

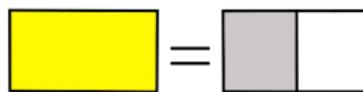
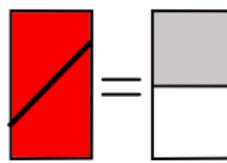
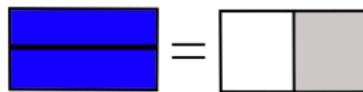
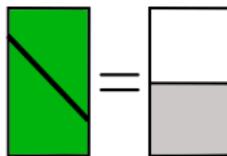


Рис. 7: Bijection between lattice-path-ensemble and domino tiling

Modified Aztec diamond II

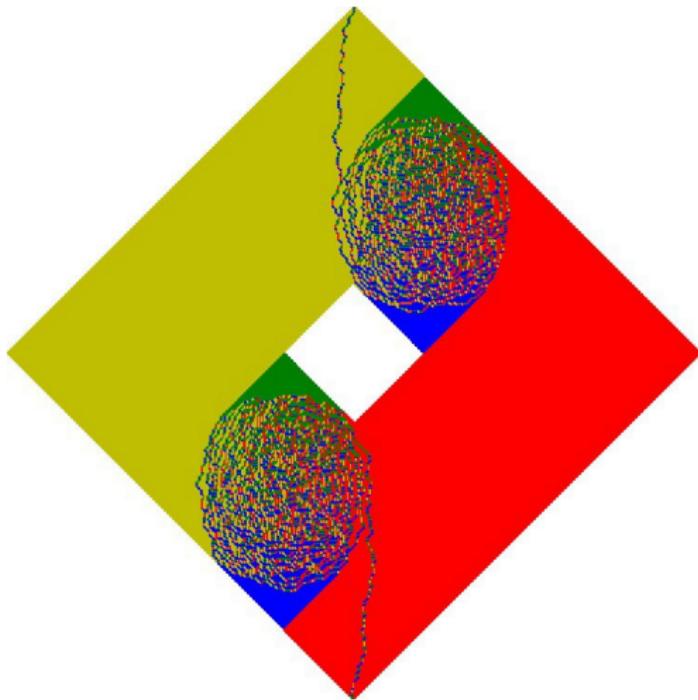
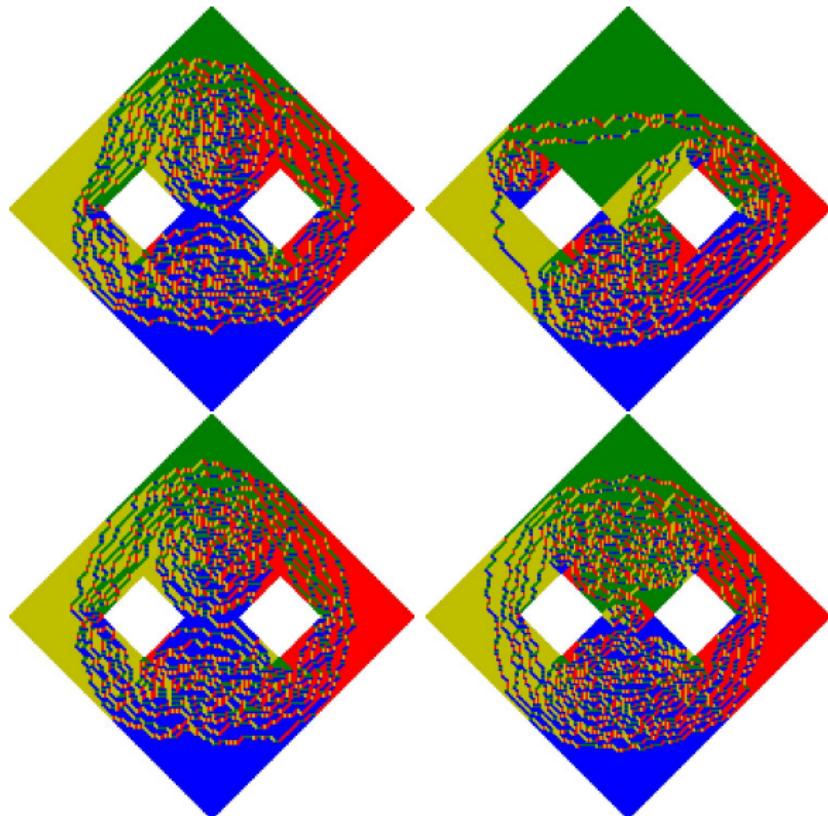


Рис. 8: A typical tiling for the maximal height change

Genus 2 case



The End